

# Molecular Clouds (1.5 weeks)

① Overview + history  
H<sub>2</sub>, CO

② Observational background

③ Emission Processes

④ Giant Molecular Clouds \* ~~Sept 30~~  
Keith

⑤ Getting physical info from lines  
LTE, LVG

⑥ Formation and destruction of molecules

⑦ Heating/cooling \*\* ~~Oct 10 - Kristen~~

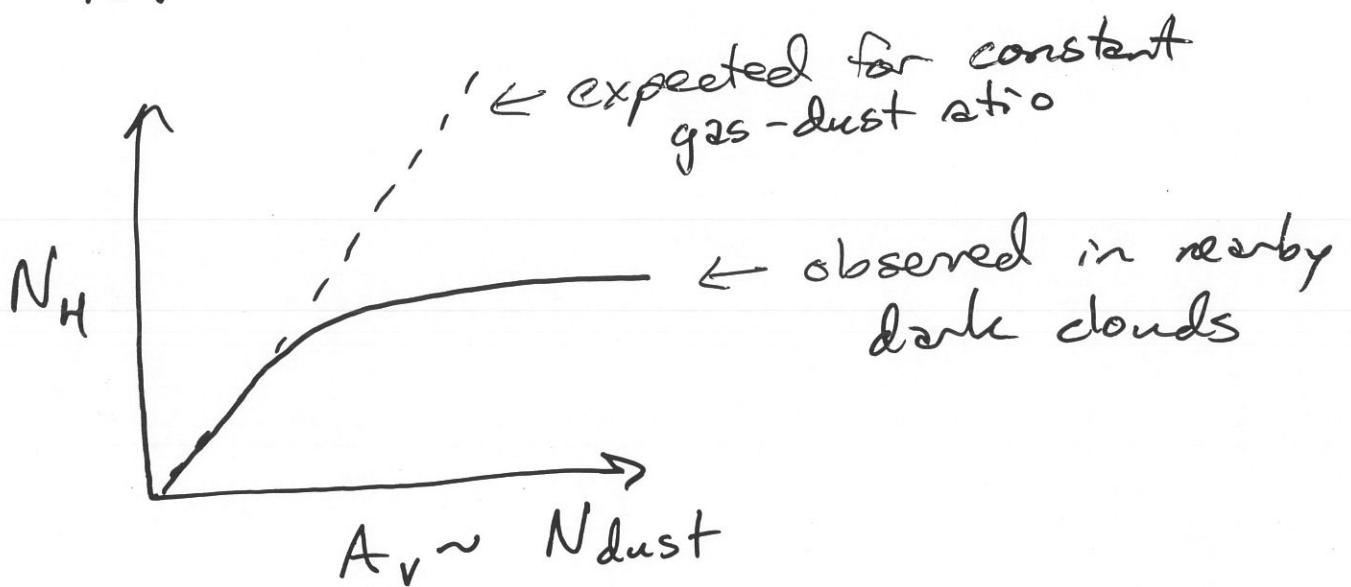
⑧ High-Latitude Clouds, Dark Clouds (if time)

\* Sanders, Scoville, & Solomon, 1985,  
ApJ, 289, 373

\*\* Goldsmith-Langer 1978, ApJ 222, 881

Existence of HI in ISM known since  
1951 (Ewen + Purcell); predicted  
~1945

Existence of  $H_2$  first inferred by Bok (1955)  
from comparing visual extinction  
 $A_v$  with HI column density  $N_{HI}$



Presence of  $H_2$  also inferred with detection  
of CO in ~1970

→ need  $n \gtrsim 10^3$  to collisionally  
excite CO

→ only  $H_2$  could contain this  
density (if HI, see it at 21cm)

H<sub>2</sub> first detected ~ 1970

- UV spectrometers above atmosphere
- nearby B stars behind cloud edge ( $A_V \lesssim 2$  mag)

⇒ did make up missing gas

H<sub>2</sub> not generally observable

→ no permanent electric dipole moment

∴ → no  $\Delta J = 1$  rotational transitions

$\Delta V = 0$      $\Delta J = 2-0$      $\lambda = 28 \mu\text{m}$  ← local atmosphere  
                  4-2                   12  $\mu\text{m}$

$\Delta V = 1$

$\lambda = 2 \mu\text{m}$

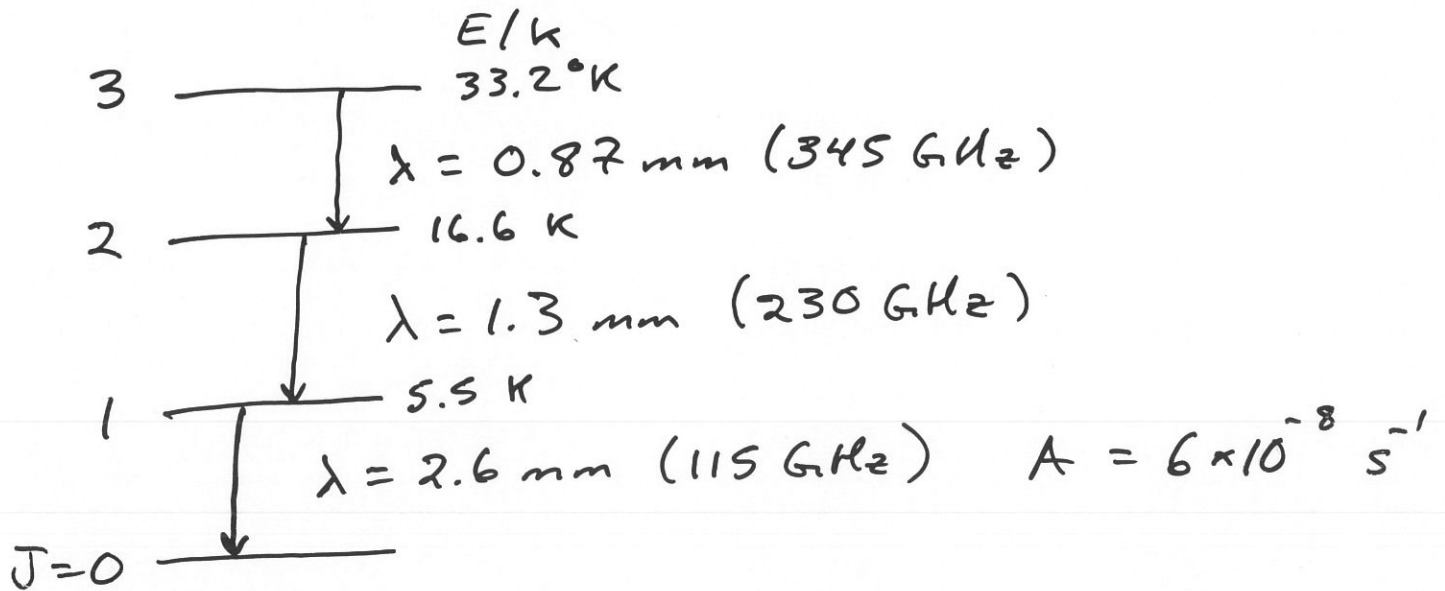
↑  
detected in shock heated gas

$T \sim 1000-2000$  K

→ need a more easily observed, common molecule to trace molecular gas

CO is abundant  $\text{CO}/\text{H}_2 \sim 10^{-4}$  in clouds (30% of C in CO)

CO has easily observed and excited transitions



- readily excited by collisions with  $\text{H}_2$ , even at low kinetic temperature  $T_k$

critical density  $n_{\text{H}_2} \gtrsim 3000 \text{ cm}^{-3}$

BUT CO is optically thick, usually ( $\tau \gtrsim 10$ )  $\rightarrow$  photon trapping

$$A \rightarrow A_{\beta} = \frac{A}{\tau} \quad \rightarrow n_{\text{H}_2, \text{crit}} \lesssim 300 \text{ cm}^{-3}$$

$^{12}\text{CO}$  emission is optically thick  
→ not good tracer of column density

However, empirically it is found to  
be a good column density  
(+ hence mass) tracer

$$N(\text{H}_2) = \alpha I_{\text{CO}} \\ \hookrightarrow \int T(\text{CO}) dV$$

#### 4 techniques

①  $^{13}\text{CO}$  vs  $^{12}\text{CO}$

②  $^{12}\text{CO}$  vs  $A_V$

③  $L(^{12}\text{CO})$  vs  $M_{\text{vir}}$

④  $\gamma$ -rays

$$\alpha \sim 2-3 \times 10^{20} \text{ cm}^{-2} (\text{K km/s})^{-1}$$

Key point is to estimate  $N(\text{H}_2)$

①  $^{13}\text{CO}$   $\rightarrow$  optically thin  
 $\rightarrow$  derive  $N(^{13}\text{CO})$  (LTE)  
 $\rightarrow$  adopt value for  $^{13}\text{CO}/\text{H}_2$   
 $\rightarrow N(\text{H}_2)$

②  $A_v \rightarrow$  assume  $N(\text{H}_2)/A_v$

④  $\gamma$ -rays  $\rightarrow$  produced when cosmic rays collide with hydrogen

If cosmic ray density is constant, observed  $\gamma$ -ray flux measures

$$n_{\text{H}} = (n_{\text{HI}} + 2n_{\text{H}_2}) \text{ in volume}$$

$\rightarrow$  compare  $\gamma$ -ray survey + HI survey to CO surveys

③ Estimate  $N(\text{H}_2)$  from virial mass and observed size

# Virial Theorem for Observers

- tend to use simplest form

$$2T = \Omega$$

↑                    ↑  
kinetic            potential  
energy             energy

$$Mv^2 = \frac{GM^2}{R} \quad \rightarrow \Delta V = \left(\frac{GM}{R}\right)^{1/2}$$

$$I_{CO} \equiv \int T_{CO} dV \quad (\text{K km s}^{-1})$$

$$L_{CO} = \Omega^2 \int I_{CO} d\Omega$$
$$\equiv T_{CO} \Delta V \pi R^2$$

$$\therefore L_{CO} = \left(\frac{3\pi G}{4}\right)^{1/2} \left(\frac{T_{CO}}{\rho^{1/2}}\right) M$$

observed brightness  
α may depend on temperature  
and density of gas

# Emission Processes

(ref's Spitzer  
bits of Ch. 2-4)

velocity distribution of particles is

Maxwellian

$$f(v) = \frac{l^3}{\pi^{3/2}} e^{-l^2 v^2}$$

velocity  
distribution  
function

$$l^2 = \frac{m}{2kT} = \frac{3}{2 \langle v^2 \rangle}$$

→ there is a characteristic (local) kinetic temperature  $T_k$

If we assume Local Thermodynamic Equilibrium (LTE), then relative populations of two levels  $j < k$  is given by

$$\frac{n_k}{n_j} = \frac{g_k}{g_j} e^{-h\nu_{jk}/kT_k}$$

Boltzmann  
equation



# Review of Basics of Radiative Transfer

Spitzer  
Ch. 3.1

$I_\nu$  = specific intensity  $\text{erg s}^{-1} \text{cm}^{-2} \text{sr}^{-1}$

$$\frac{dI_\nu}{ds} = -K_\nu I_\nu + j_\nu$$

$\uparrow$  absorption coefficient       $\uparrow$  emission coefficient

$$d\tau_\nu = -K_\nu ds$$

$\uparrow$  optical depth

$\rightarrow \tau_\nu = 0$  at observer  
 $K_\nu > 0$ ,  $\tau_\nu$  increases towards source

Radiation received from cloud of total optical depth  $\tau_\nu$

$$I_\nu = I_\nu(0) e^{-\tau_\nu} + \int_0^{\tau_\nu} \frac{j_\nu}{K_\nu} e^{-\tau_\nu} d\tau_\nu$$

$I_\nu(0)$   $\rightarrow$  value of  $I$  on far side of emitting region

(ie a continuum source in background microwave background at 3K)

In thermodynamic equilibrium

$$I_\nu = B_\nu(T) = \frac{2h\nu^3}{c^2} \frac{1}{e^{h\nu/kT} - 1}$$

( $T$  is the kinetic temperature of gas)

if  $I_\nu = \text{const}$ ,  $dI_\nu/ds = 0$

$\rightarrow j_\nu = K_\nu B_\nu(T)$  Kirchhoff's law

if  $T$  is constant over path length

$$I_\nu = I_\nu(0) e^{-\tau_\nu} + B_\nu(T) (1 - e^{-\tau_\nu})$$

if  $h\nu/kT \ll 1$

$$B_\nu(T) = \frac{2\nu^2 kT}{c^2}$$

Rayleigh-Jeans Law

$$\frac{h\nu}{kT} = \frac{14.39}{\lambda(\text{mm}) T(\text{K})}$$

$\rightarrow$  not a good approximation in millimeter and submillimeter

$I_\nu$  is frequently replaced by the  
"brightness temperature"  $T_B$

$$B_\nu(T_B) \equiv I_\nu$$

If Rayleigh-Jeans law applies, get

$$T_B = T_B(0) e^{-\tau} + T(1 - e^{-\tau})$$

↑  
observed  
brightness  
temperature

↑  
brightness  
temperature  
incident  
on far side  
of cloud

↑  
kinetic temperature  
of cloud

ignoring  $T_B(0)$  for the moment

$$\tau \gg 1 \quad \rightarrow \quad T_B = T$$

$$\tau \ll 1 \quad \rightarrow \quad T_B = \tau T$$

# Collisional Excitation

① Consider a simple, 2-level system  
transition  
collision rate / sec / molecule

$$C_{ul} \equiv C_{u \rightarrow l} = n \gamma_{ul} \quad \begin{array}{l} \text{rate coefficient} \\ \text{density (of } H_2 \text{)} \end{array}$$

$$C_{lu} = C_{ul} \frac{g_u}{g_l} \exp\left(\frac{-h\nu}{kT_k}\right)$$

→ straight forward to calculate populations

$n_u$  and  $n_l$  ( $n_{tot} = n_u + n_l$ ) from  
detailed balance, given  $\gamma_{ul}$ ,

$A_{ul}$ ,  $T_k$ ,  $n$

$$n_l (\gamma_{lu} n) = n_u (\gamma_{ul} n + A_{ul})$$

or

$$\frac{n_u}{n_{tot}} = \frac{\frac{g_u}{g_l} \exp\left(\frac{-h\nu}{kT_k}\right)}{1 + \frac{g_u}{g_l} \exp\left(\frac{-h\nu}{kT_k}\right) + \frac{n_{crit}}{n}}$$

$n_{crit} = A_{ul} / \gamma_{ul}$  "critical density"

critical density is a key parameter  
 → can collisions keep up with  
 spontaneous radiation?

$n \gg n_{crit}$  → level populations are thermalized

$$\left( \frac{n_u}{n_l} \right)_{\text{thermal}} = \frac{g_u}{g_l} \exp\left(-\frac{h\nu}{kT_e}\right)$$

below critical density, spontaneous  
 radiative rates are faster than collisions  
 → population is "subthermal"

$$\frac{n_u}{n_l} = \frac{n}{n_{crit}} \left( \frac{n_u}{n_l} \right)_{\text{thermal}}$$

For multi-level system

$$n_u \left\{ \sum_{k \neq u} (n \gamma_{uk} + B_{uk} U_\nu) + \sum_{k < u} A_{uk} \right\}$$

$$= \sum_{u \neq k} n_k (n \gamma_{ku} + B_{ku} U_\nu) + \sum_{k > u} A_{ku} n_k$$

$$u_\nu = \frac{1}{c} \int I_\nu d\omega$$

energy density  
per unit frequency

If the emission from a line is optically thick, then the level populations may be thermalized at lower densities due to photon trapping

photon escape probability  $\beta \sim \frac{1}{\tau}$

$$\tau \ll 1 \rightarrow I_{\text{thin}} \propto n_u V A$$

$$\tau \gg 1 \rightarrow I_{\text{thick}} \propto n_u V A \beta$$

ie, effectively

$$A \rightarrow A \beta \sim \frac{A}{\tau}$$

The velocity dispersion  $\sigma$  is plotted against the maximum linear dimension  $L$  of molecular clouds and condensations, based on data from Table 1. A well-defined correlation between  $\log \sigma$  and  $\log L$  is seen, and within the scatter it is well represented by the eye-fitted dashed straight line, whose equation is

$$\sigma (\text{km s}^{-1}) = 1.10 L (\text{pc})^{0.38} \quad (1)$$

The rms deviation of  $\log \sigma$  from this relation is 0.14, corresponding to a factor of 1.38 in  $\sigma$ . Equation (1) holds for  $0.1 \leq L \leq 100$  pc, and is almost identical to the relation  $\sigma = 1.1 L^{0.38}$  found by Larson (1979) for interstellar motions on somewhat larger length scales,  $1 \leq L \leq 1000$  pc; this earlier study included fewer data on molecular clouds, but some data on H I cloud velocities and larger-scale streaming motions. The present result strengthens the conclusion that the velocity dispersion of interstellar motions shows a general power-law correlation with region size, and extends it to smaller length scales.

The data in Table 1 show, moreover, that a similar relation between  $\sigma$  and  $L$  often holds even within individual clouds. Fig. 2 shows the variation of  $\sigma$  with  $L$  in all of the clouds of complexes for which at least one subregion is listed in Table 1; in this diagram straight lines connect the symbols for each subregion and the larger cloud of which it is a part. The velocity dispersions of groups of T Tauri stars in the Taurus clouds (Table 1 and Jones & Herbig 1979) are also plotted as asterisks in Fig. 2(a). The left part of Fig. 2(b) shows additional data for several dark clouds as reproduced from Fig. 89 of Snell (1979); in this

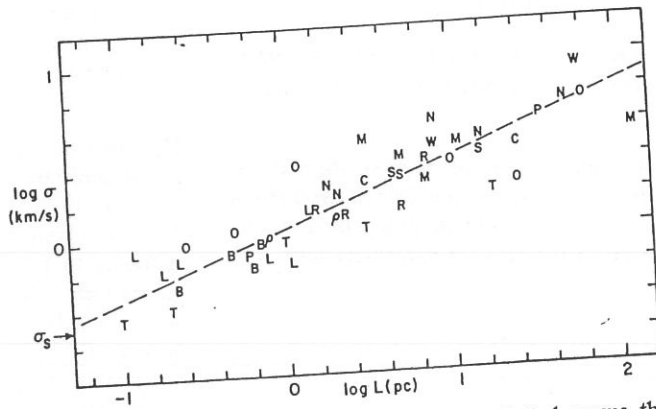


Figure 1. The three-dimensional internal velocity dispersion  $\sigma$  plotted versus the maximum linear dimension  $L$  of molecular clouds and condensations, based on data from Table 1; the symbols are identified in Table 1. The dashed line represents equation (1), and  $\sigma_s$  is the thermal velocity dispersion.

Larson 1981  
MNRAS

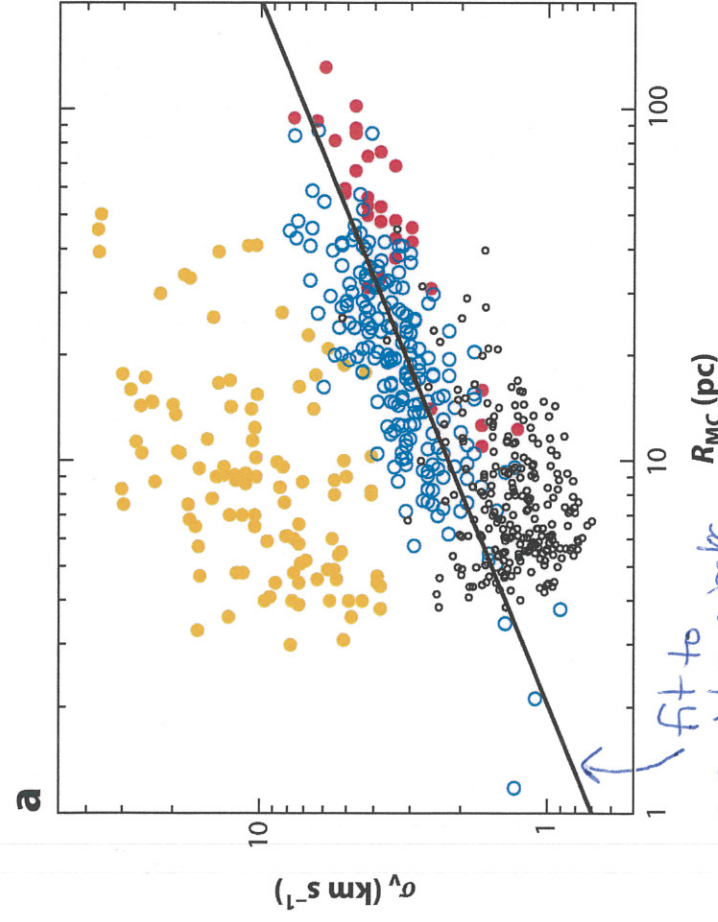
$\sigma \propto L^{0.38}$   
(by-eye fit)

compare to

Kolmogoroff law  $\sigma \sim L^{1/3}$   
(subsonic turbulent flows)

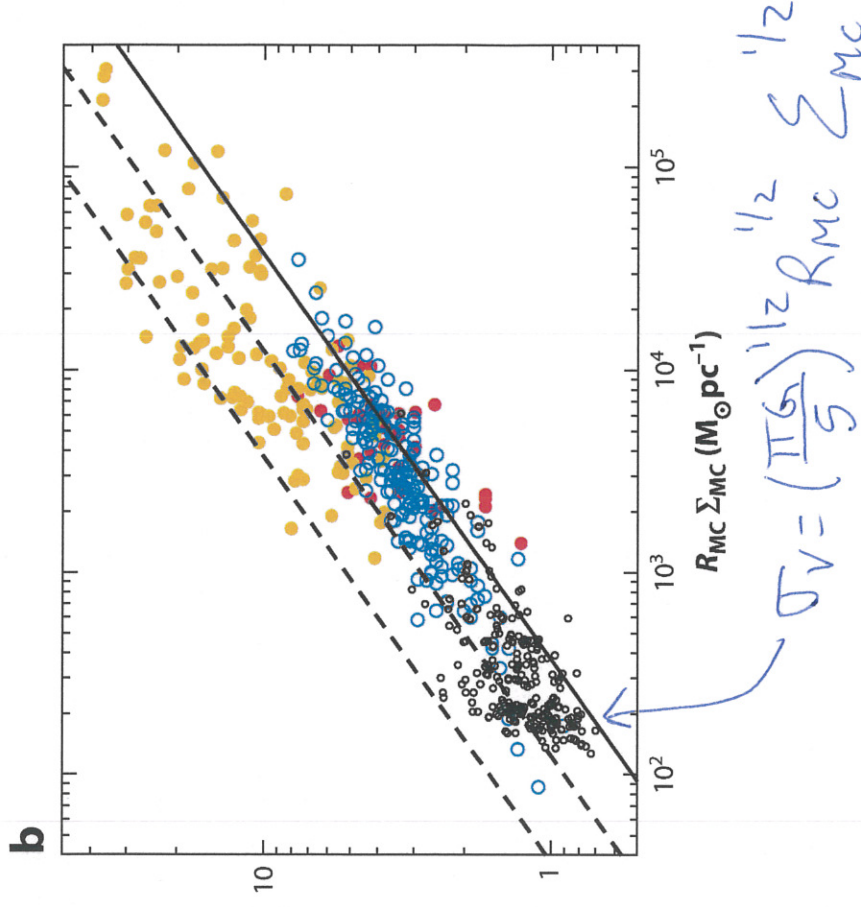
$\sigma$  vs  $M$  implies most regions are gravitationally bound and roughly in virial equilibrium





Heyer M, Dame TM. 2015.

Annu. Rev. Astron. Astrophys. 53:583-629



- gold dots are clouds near Galactic Center

- equation for line in right panel is virial theorem (grav and kinetic energy equipartition)

+ Larson's Law with exponent 0.5



# Overview of Properties of Giant Molecular Clouds

see Fukui & Kawamura, 2010, ARAA, 48 547

- masses from  $10^4$  - few  $\times 10^6 M_{\odot}$

- (linewidth)  $\Delta V \propto R^{0.5}$  (size)

→ for virialized clouds implies

$$\bar{n} \propto 1/R$$

$$\bar{N} = \text{constant}$$

- ~~mass~~ function  $\frac{dN}{dm} \propto M^{-1.7}$

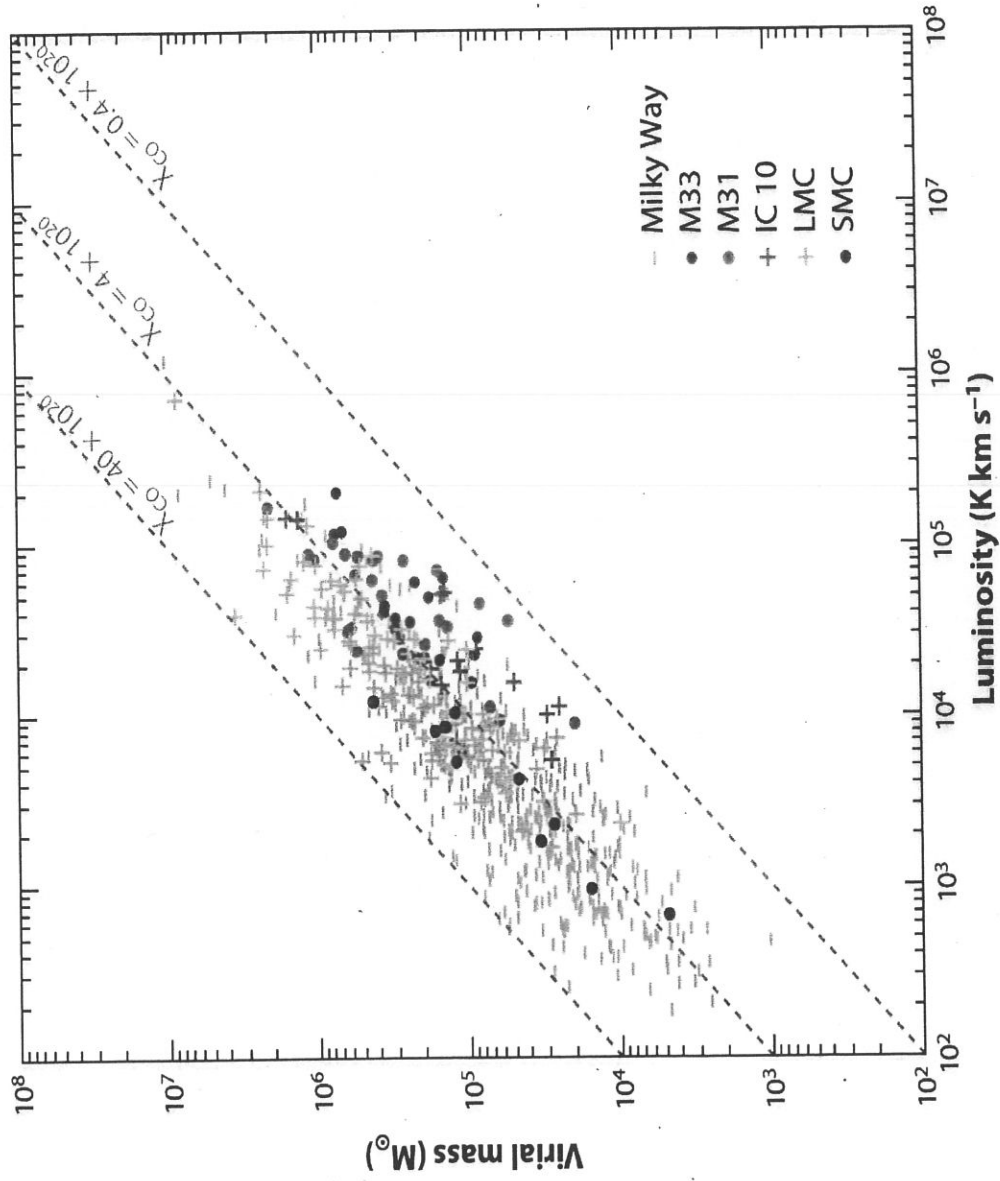
→ implies most mass is in the few largest clouds

Linewidths  $\gg$  thermal linewidths (1-10 km/s)

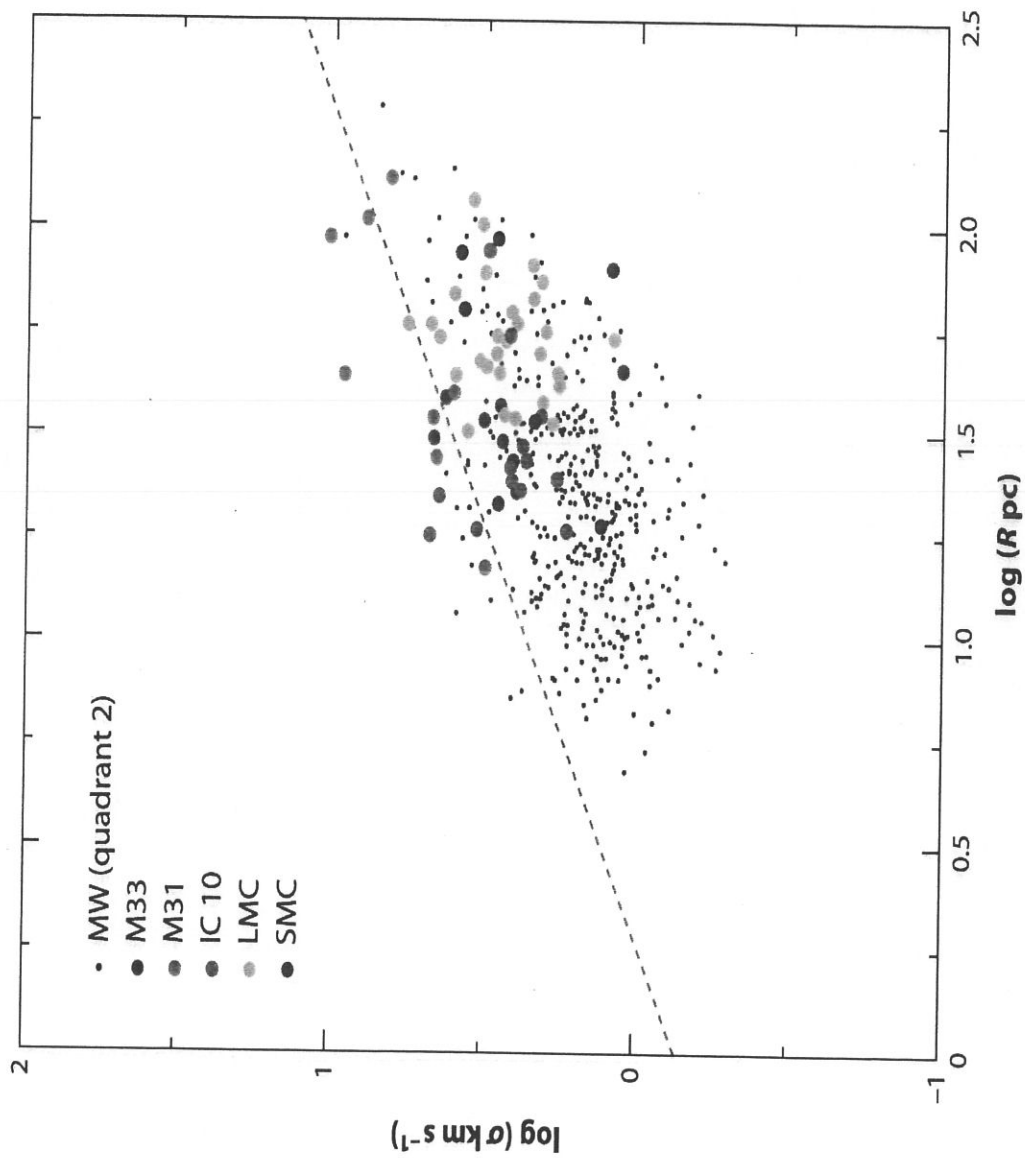
Sizes 10-100 pc

Low star formation efficiency (few percent)

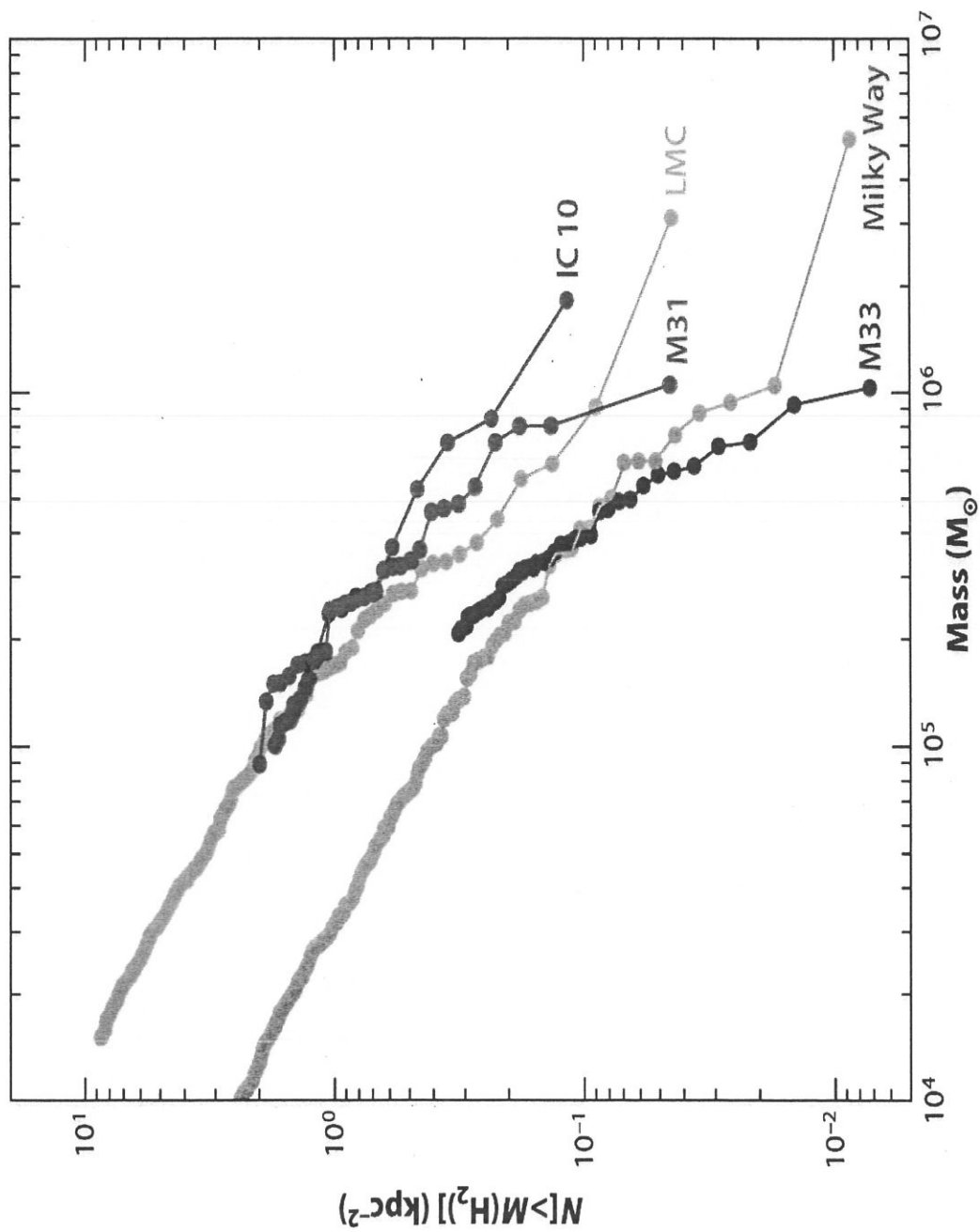
See Figures 2, 3 & 4 (not copied)



 Fukui Y, Kawamura A. 2010.  
 Annu. Rev. Astron. Astrophys. 48:547–80



Fukui Y, Kawamura A. 2010.  
Annu. Rev. Astron. Astrophys. 48:547–80



**AR** Fukui Y, Kawamura A. 2010. Annu. Rev. Astron. Astrophys. 48:547–80